

# MODELING OF A WIND ENERGY CONVERSION SYSTEM FOR DYNAMIC ANALYSIS USING ATP

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**Abstract** - In recent decades wind energy has gained great prominence in various parts of the world. This fact shows the need to develop advanced studies in order to evaluate the dynamic behavior of modern wind turbines. Within this context, this work presents a mathematical and computer modeling in ABC reference frame of a Wind Energy Conversion System (WECS) using a Permanent Magnet Synchronous Generator (PMSG). The functionality of the constructed model is verified through computer simulations of wind turbulences and load changes using the free software Alternative Transients Program (ATP), especially with its MODELS interface.

**Keywords** – ATP, Load changes, PMSG, WECS.

## I. INTRODUCTION

Wind energy is a green and renewable energy source with low operation cost and it has played an important role in power grid expansion in several countries, totaling 283 GW of worldwide installed capacity in 2012, which is 45 GW larger than in 2011 [1].

Talking about modern wind systems, Permanent Magnet Synchronous Generators (PMSG) have been frequently used in variable speed wind turbines [2, 3] mainly because a gearbox installation is not required, thereby reducing weight, cost and maintenance [4], providing higher reliability and decreasing noise emissions during low speed operation [5]

Additionally, when a PMSG is connected to a frequency conversion electronic system, voltage regulator and turbine governor are eliminated, enabling the adjustment of active and reactive power injected into power grid and the maintenance of voltage and frequency levels within appropriate ranges [6].

This scenery has led to the development of many researches about the dynamic behavior of PMSG-based wind turbines, where its mathematical modeling has been chiefly carried out in the DQ0 reference frame. Computer simulations are normally performed using MatLab [7, 8, 9] and including wind variations. Eventually, other associated computer programs are adopted to represent the wind and turbine mechanical parts [9].

Alternative Transients Program (ATP), a free distribution version of its precursor Electromagnetics Transients Program (EMTP), has gained a great prominence in commercial, academic and scientific scope around the world. This computer platform provides time domain techniques functions, mainly through its ATPDraw and MODELS interfaces, which are appropriate features for modeling the whole Wind Energy Conversion System (WECS). Besides, ATP offers excellent graphics capabilities and a friendly interaction with the user. Thereby, these attributes have motivated the utilization of ATP for computer simulations presented in this work.

This paper presents a mathematical and computer modeling of a WECS with a PMSG-based wind turbine supplying an isolated load. The ABC reference frame is used instead of DQ0 system especially because real generator parameters are better employed in such representation. The functionality of the implemented modeling is verified through computer studies performed with ATP taking into account normal and abnormal wind speed conditions, besides sudden load changes.

## II. MATHEMATICAL MODELING

Figure 1 presents the electromechanical topology of WECS focused in this work.

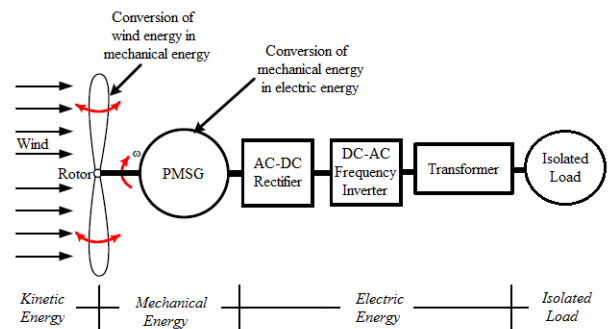


Fig. 1. Electromechanical topology of WECS

### A. Wind Model

The mathematical formulation  $v_{wind}$  chosen for representing the wind speed in this work is a four-component model defined by equation (1), as described in [10]. This expression is attractive since it expresses both the natural intensity of primary energy source as well as the possible occurrence of wind turbulences, including its random component.

$$v_{wind} = v_{base} + v_{gust} + v_{ramp} + v_{noise} \quad (1)$$



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Where:

- $v_{base}$ : base wind speed component [m/s];
- $v_{gust}$ : gust wind speed component [m/s];
- $v_{ramp}$ : ramp wind speed component [m/s];
- $v_{noise}$ : noise wind speed component [m/s].

As ATPDraw libraries do not provide the adopted wind model, it was necessary to develop it using the MODELS interface that uses a structured programming language similar to FORTRAN. This alternative allowed the production of a new block component representing the wind and its variations.

### B. Wind Turbine Model

The wind turbine is mainly composed by the rotor and the blades and it plays an important role in wind energy conversion. It is responsible by extracting power from the wind and passing it on to the electric generator shaft [11].

It is well known that the wind kinetic energy ( $J/m^3$ ) is given by equation (2).

$$E = \frac{1}{2}mv_{wind}^2 \quad (2)$$

Where:

- $v_{wind}$ : wind speed [m/s];
- $m$ : mass of air [kg].

This equation can be represented in the form of wind power  $P_{wind}$  (Watts) by equation (3).

$$P_{wind} = \frac{1}{2}\rho Av_{wind}^3 \quad (3)$$

Where:

- $A$ : área swept by turbine blades [ $m^2$ ];
- $\rho$ : air density ( $\rho = 1.225$  for standard pressure at sea level and 25 C) [ $kg/m^3$ ].

Not all the power provided by wind can be used by the turbine. For this reason, equation (4) expresses the power coefficient or performance coefficient  $C_p$ , which is the ratio between the mechanical power available in the turbine shaft  $P_{mec}$  and the wind power  $P_{wind}$ .

$$C_p = \frac{P_{mec}}{P_{wind}} \quad (4)$$

From equations (3) and (4), the mechanical power extracted from wind and used by turbine is obtained (5).

$$P_{mec} = \frac{1}{2}C_p(\lambda, \beta)\rho Av_{wind}^3 \quad (5)$$

Where:

- $\lambda$ : tip speed ratio [dimensionless];
- $\beta$ : blade pitch angle [degrees].

Tip speed ratio  $\lambda$  is defined by equation (6):

$$\lambda = \frac{v_{blade}}{v_{wind}} = \frac{\omega_R R}{v_{wind}} \quad (6)$$

Where:

- $v_{blade}$ : turbine blade tip speed [m/s];
- $R$ : rotor radius [m];
- $\omega_R$ : rotor angular speed [rad/s]

Figure 2 illustrates the block diagram of pitch angle control which is intended to limit the mechanical power transferred to the PMSG. Thus, it ensures that wind turbine power is kept close to its rated value for very high wind speeds [12]. If the wind speed reaches a value above the turbine cut-off limit, then PMSG is turned-off.

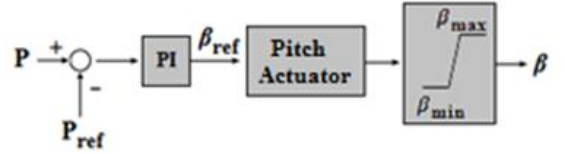


Fig. 2. Pitch angle control block diagram

Again, as the adopted wind turbine model is not available in ATPDraw libraries, it was necessary to develop it using the MODELS interface. Thus, a new block component representing the wind turbine was also constructed and connected to the wind block.

### C. PMSG Model

This work employs a synchronous generator with a high number of poles because of low rotational speeds derived from its direct connection to the wind turbine shaft. The machine comprises 3-phase armature windings at stator and a permanent magnet field at rotor to ensure a constant magnetic flux. This last feature avoids the need of a DC excitation source.

An arrangement of the PMSG with only two poles is shown in Figure 3, where  $aa'$ ,  $bb'$ ,  $cc'$  represent the armature windings placed at machine stator.

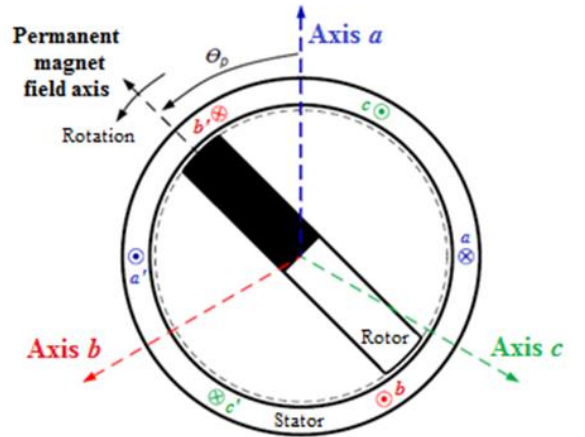


Fig. 3. PMSG physical topology

The PMSG model is based on linkage flux expressions of conventional synchronous machine [13, 14] employing modeling techniques in ABC reference frame. It is important

to point that some adjustments were performed in order to consider the flux produced by the rotor permanent magnet. This strategy modified the conventional synchronous machine equations where rotor magnetic field is produced by DC excitors.

As ATPDraw libraries do not include the above mentioned PMSG model, once more it was necessary to create it by the MODELS interface. Thus, a new block component representing the PMSG was also built and connected to the wind turbine block.

#### D. AC-DC Uncontrolled Rectifier and DC Link Models

The full-wave rectifier and the DC link are represented by an uncontrolled 6-pulse 3-phase diode bridge and an output capacitor, respectively, as shown in Figure 4.

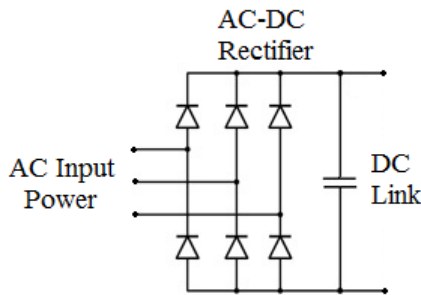


Fig. 4: Full-wave rectifier and the DC link topology

Further details about these devices are not presented since all their components (diodes, resistors and capacitors) are readily available in ATPDraw libraries and widespread in the related literature.

#### E. Frequency Inverter Model

The 3-phase frequency inverter considered in this work comprises six controlled thyristors, as illustrated in Figure 5, and produces an AC voltage system, from DC link voltage, which will be connected to the local grid. As this device represents an important unit for the integration of wind farms to both power grid and isolated loads, its control system must be configured so as to obtain an appropriate interconnection in either steady-state or dynamical condition.

In this work, the classical vector control strategy is used for the definition of the firing logic requirements for the six thyristors [15]. Besides, using the PWM technique, also widely applied in this study field, the 6-thyristor firing sequence is achieved, thereby determining the characteristics of the 3-phase voltage produced at the inverter output terminals [16].

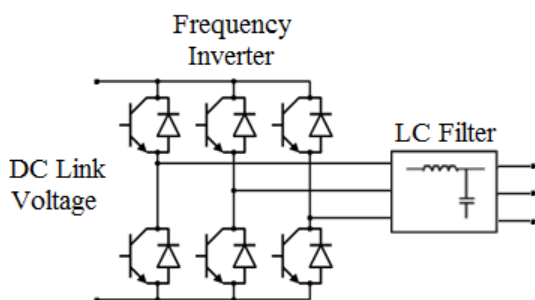


Fig. 5: Frequency inverter topology

Figure 6 depicts the block diagram of load voltage magnitude control performed by frequency inverter, which allows the maintenance of load voltage levels within appropriate ranges even under wind speed variations and sudden load changes. From monitoring the isolated load voltage, the control system defines the variation of the inverter modulation factor ( $m_p$ ), which will act to increase/decrease the AC voltage produced at its terminals.

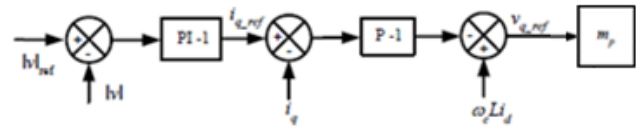


Fig. 6: Block diagram of load voltage magnitude control

The inverter modulation factor is calculated according to equation (7). It is also important to mention that, at the output terminals of the frequency inverter, an LC filter is connected, whose role is to filter the voltage wave obtained, bringing it much closer to sinusoidal shape.

$$m_p = \frac{1}{v_{q\_ref}} \quad (7)$$

The required components (thyristors, resistors and capacitors) for the construction of frequency inverter electric circuit are readily available in ATPDraw libraries. However, the development of two new blocks by MODELS interface is necessary: the first one to take into account the load voltage magnitude control strategy; and the second one to represent the 6-thyristor firing PWM technique. The frequency inverter electric arrangement, including the two new control blocks, is connected just after the DC link.

#### F. Transformer Model

The transformer works to raise the frequency inverter output voltage to a suitable value demanded by isolated loads. In addition, when wind farms are connected to large power grids, the transformer increases this voltage value to comply with power transmission common ranges.

This work employs a 2-winding transformer, whose model is readily available in ATPDraw libraries, including the nonlinear feature of core ferromagnetic material, but such effect was disregarded since it is not a major influence on the objectives sought here. Further details about this device are not presented because transformer modeling and operation are widespread in the literature.

#### G. Isolated Load Model

As mentioned, the WECS modeled in this work supplies a 3-phase isolated load, which is characterized as having an inductive power factor of 0.92. This value is chosen so as to represent a real industrial load connected to a distribution power system. The load components (resistors and inductors) are readily available in ATPDraw libraries, not requiring further information about their models.

### III. COMPUTER STUDIES

This section aims to present the computer studies performed to verify the functionality of the mathematical models presented for the WECS and to evaluate the load voltage magnitude control developed. For that, simulations were performed using Alternative Transients Program (ATP), considering the overall electric system under distinct operating conditions.

The parameters of wind turbine and PMSG models, used in this work, are listed in Tables 2 and 3, respectively.

Table 2: Wind turbine parameters

|                                                       |                    |
|-------------------------------------------------------|--------------------|
| Wind turbine rated power (MW)                         | 2                  |
| Rotor diameter (m)                                    | 62                 |
| Rated wind speed (m/s)                                | 13.52              |
| Turbine inertia moment ( $\text{kg}\cdot\text{m}^2$ ) | $2.92 \times 10^6$ |

Table 3: PMSG parameters

|                                              |       |
|----------------------------------------------|-------|
| PMSG rated power (MW)                        | 2     |
| PMSG rated voltage (kV)                      | 690   |
| PMSG rated frequency (Hz)                    | 13    |
| PMSG number of poles                         | 64    |
| Stator winding resistance (p.u.)             | 0.042 |
| Direct axis reactance (p.u.)                 | 1.05  |
| Quadrature axis reactance (p.u.)             | 0.75  |
| Magnetic flux of rotor permanent magnet (Wb) | 7     |

#### A. Wind Disturbances

Figure 7 illustrates the wind behavior considered for computer simulations. Initially, the wind speed was set at its optimal value of 13.52 m/s. During the time period from  $t = 10$  s to  $t = 20$  s, a positive wind gust with maximum speed rise of 4 m/s was applied. Later, at  $t = 35$  s, a negative wind ramp was started, which reached a maximum speed drop of 2 m/s at  $t = 43$  s.

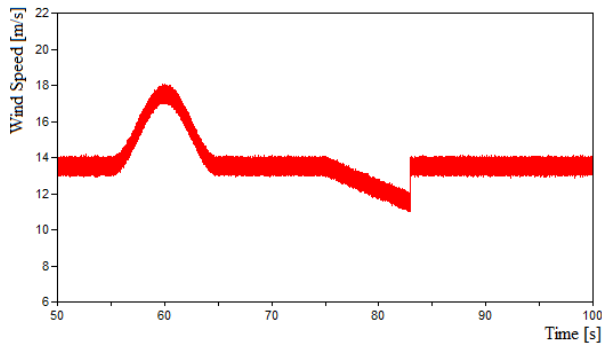


Fig. 7: Wind speed behavior

Figure 8 depicts the mechanical speed of the wind turbine rotor, while Figure 9 shows the corresponding terminal voltage frequency produced by PMSG. The solid lines indicate that prior to the occurrence of the wind disturbances, i.e., in steady state condition, the angular speed of the rotor was 3.7 rad/s, corresponding to the electric frequency of 18.7 Hz. Although the PMSG rated electric frequency was

13.0 Hz, a larger electric frequency was obtained since that the load supplied by the wind generator was below its rated value.

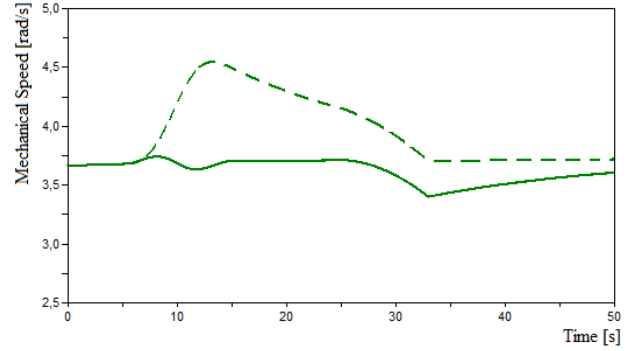


Fig. 8: Mechanical speed behavior

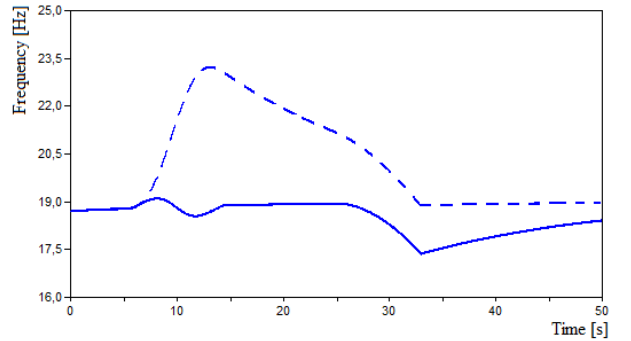


Fig. 9: PMSG terminal voltage frequency behavior

The occurrence of the positive wind gust caused the operation of the pitch control, which achieved a maximum angle of approximately  $18.0^\circ$ , as illustrated in Figure 10, following the wind behavior. This fact resulted in attenuation of both mechanical speed and PMSG voltage frequency rises, which started at  $t = 10$  s in Figures 8 and 9, respectively. The dotted curves illustrate that such variables would have an increase of approximately 22% if the pitch control was turned off.

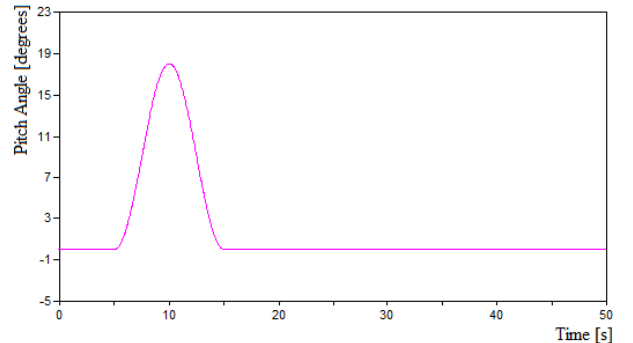


Fig.10: Pitch control behavior

During the presence of negative wind ramp, there was a reduction of rotor speed and voltage frequency supplied by PMSG, which reached minimum values of 3.41 rad/s and 17.4 Hz, respectively, as seen in Figures 8 and 9.

Figure 11 shows that the DC link voltage in steady state condition was 1420 V, approximately. The wind gust caused

the operation of the pitch control, which allowed the maintenance of DC voltage close to the steady state value. However, the negative wind ramp caused a DC voltage decline to about 1350 V. The dotted line illustrates the DC link voltage behavior if the pitch control was turned off, achieving a maximum value close to 1720 V.

The dotted curve from Figure 12 illustrates the isolated load voltage when both frequency inverter and pitch controls were turned off. In steady state condition the load voltage was 13.8 kV and, during the positive wind gust, it achieved 16.2 kV, whereas at the end of the negative wind ramp it dropped to 13.4 kV. The solid line indicates that the load voltage could be maintained at 13.8 kV if both frequency inverter and pitch controls were enabled.

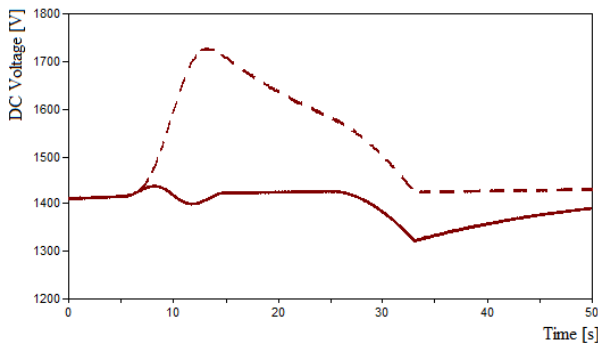


Fig. 11: DC link voltage behavior

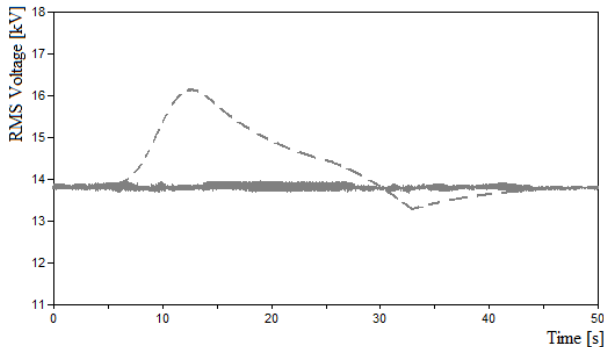


Fig. 12: Isolated load voltage behavior

### B. Sudden Load Changes

This section shows the voltage behavior for distinct sudden load changes taking into account a constant base wind speed of 13.52 m/s, including the noise component, as illustrated in Figure 13. It is important to mention that other WECS variables, such as turbine mechanical speed and PMSG voltage frequency, will have similar variations and, therefore, they need not to be presented here. Initially, the load was 1.587 MVA, with approximately 0.92 power factor. At  $t = 10$  s there was 20% load shedding, which decreased the power value to about 1.270 MVA. Later, at  $t = 35$  s, this load was increased by 30%, raising the power value to 1.650 MVA.

The dotted curve from Figure 14 illustrates the isolated load voltage for both frequency inverter and pitch controls switched off. In steady state condition the load voltage was 13.8 kV and, after the load shedding, it increased to a value near to 16.5 kV. On the other hand, after the load increase,

the voltage decreased to a value close to 13.2 kV. The solid line indicates that the load voltage could be maintained at 13.8 kV if both frequency inverter and pitch controls were switched on.

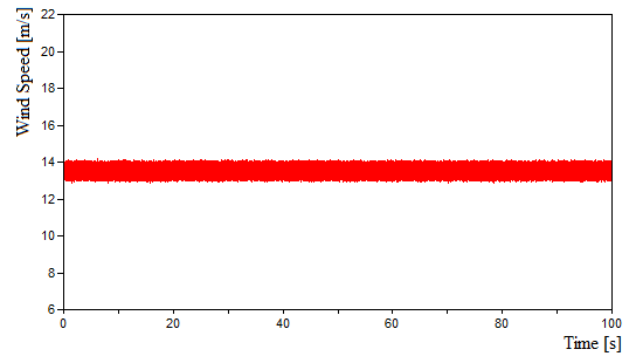


Fig. 13: Wind speed behavior

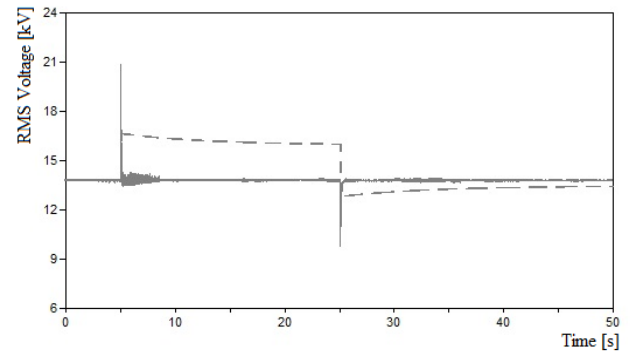


Fig. 14: Isolated load voltage behavior

## IV. CONCLUSIONS

This paper presented the mathematical and computational modeling in ABC reference frame of a Wind Energy Conversion System (WECS) equipped with a Permanent Magnet Synchronous Generator (PMSG), supplying an isolated load with 0.92 power factor. The objective of this work was to present the overall modeling developed for the WECS and to analyze the operation of pitch and frequency inverter controls to face sudden changes in wind or load.

Firstly, changes in base wind speed were simulated to represent a positive gust and a negative ramp. In both cases the operation of the frequency inverter control ensured the isolated load voltage to be kept in its rated value. The occurrence of positive wind gust also caused the pitch control operation and, consequently, maximum values for mechanical speed and turbine power could be achieved. However, such action was not performed during the negative wind ramp as expected since the maximum power limit was not exceeded.

Therefore, it was shown that the rated (maximum) WECS operation condition was tracked by the pitch control under the event of wind speed increase. It was also pointed out that the absence of such control could cause a large rise in both rotor speed and PMSG voltage frequency, which would eventually provoke electrical and mechanical damages in the wind turbine-generator set.

Secondly, distinct sudden load changes were simulated during a constant base wind speed scenario. It was noted that, when both pitch and frequency inverter controls were turned off, the partial load shedding would cause an elevation of the isolated load voltage, while a load increase would lead to a voltage rise. However, when the pitch and frequency inverter controls were enabled, the load voltage could be kept close to the rated value (13.8 kV) in both situations.

The developed mathematical modeling of the PMSG-based wind turbine in ABC system has shown to be a feasible technique for dynamic analysis of wind generators. Besides, the operation of the pitch and frequency inverter controls was able to maintain an appropriate voltage level for the isolated load.

The behavior of the main parameters related to the WECS performance (rotor speed, PMSG voltage frequency, pitch control angle, load voltage) in face of significant variations of wind speed (gust and ramp) or load power confirmed the efficiency of the developed modeling. Therefore, the free software Alternative Transients Program (ATP), especially through its MODELS interface, allowed the development of adequate representations for all WECS components.

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